

Example Candidate Responses

Cambridge International AS and A Level Mathematics

9709

Paper 7





Contents

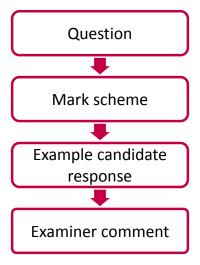
Introduction	2
Assessment at a glance	3
Paper 7	5

Introduction

The main aim of this booklet is to exemplify standards for those teaching Cambridge International AS & A Level Mathematics (9709), and to show how different levels of candidates' performance relate to the subject's curriculum and assessment objectives.

In this booklet candidate responses have been chosen to exemplify a range of answers. Each response is accompanied by a brief commentary explaining the strengths and weaknesses of the answers.

For ease of reference the following format for each component has been adopted:



Each question is followed by an extract of the mark scheme used by examiners. This, in turn, is followed by examples of marked candidate responses, each with an examiner comment on performance. Comments are given to indicate where and why marks were awarded, and how additional marks could have been obtained. In this way, it is possible to understand what candidates have done to gain their marks and what they still have to do to improve them.

Past papers, Examiner Reports and other teacher support materials are available on Teacher Support at https://teachers.cie.org.uk

Assessment at a glance

The 7 units in the scheme cover the following subject areas:

- Pure Mathematics (units P1, P2 and P3);
- Mechanics (units M1 and M2);
- Probability and Statistics (units S1 and S2).

Centres and candidates may:

- take all four Advanced (A) Level components in the same examination session for the full A Level.
- follow a staged assessment route to the A Level by taking two Advanced Subsidiary (AS) papers
 (P1 & M1 or P1 & S1) in an earlier examination session;
- · take the Advanced Subsidiary (AS) qualification only.

AS Level candidates take:

Paper 1: Pure Mathematics 1 (P1)

1¾ hours

About 10 shorter and longer questions 75 marks weighted at 60% of total

plus one of the following papers:

Paper 2: Pure Mathematics 2 (P2)	Paper 4: Mechanics 1 (M1)	Paper 6: Probability and Statistics (S1)
1¼ hours About 7 shorter and longer questions 50 marks weighted at 40% of total	1¼ hours About 7 shorter and longer questions 50 marks weighted at 40% of total	1¼ hours About 7 shorter and longer questions 50 marks weighted at 40% of total

A Level candidates take:

Paper 1: Pure Mathematics 1 (P1)	Paper 3 Pure Mathematics 3 (P3)	
1% hours About 10 shorter and longer questions 75 marks weighted at 30% of total	1¾ hours About 10 shorter and longer questions 75 marks weighted at 30% of total	

plus one of the following combinations of two papers:

Paper 4: Mechanics 1 (M1)	Paper 6: Probability and Statistics 1 (S1)	
1¼ hours About 7 shorter and longer questions	1¼ hours About 7 shorter and longer questions	
50 marks weighted at 20% of total	50 marks weighted at 20% of total	

or

Paper 4: Mechanics 1 (M1)	Paper 5: Mechanics 2 (M2)
1% hours About 7 shorter and longer questions 50 marks weighted at 20% of total	1¼ hours About 7 shorter and longer questions 50 marks weighted at 20% of total

or

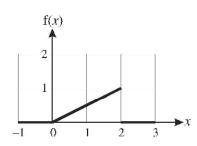
Paper 6: Probability and Statistics 1 (S1)	Paper 7: Probability and Statistics 2 (S2)
1¼ hours About 7 shorter and longer questions 50 marks weighted at 20% of total	1¼ hours About 7 shorter and longer questions 50 marks weighted at 20% of total

Teachers are reminded that the latest syllabus is available on our public website at **www.cie.org.uk** and Teacher Support at **https://teachers.cie.org.uk**

Paper 7

Question 1

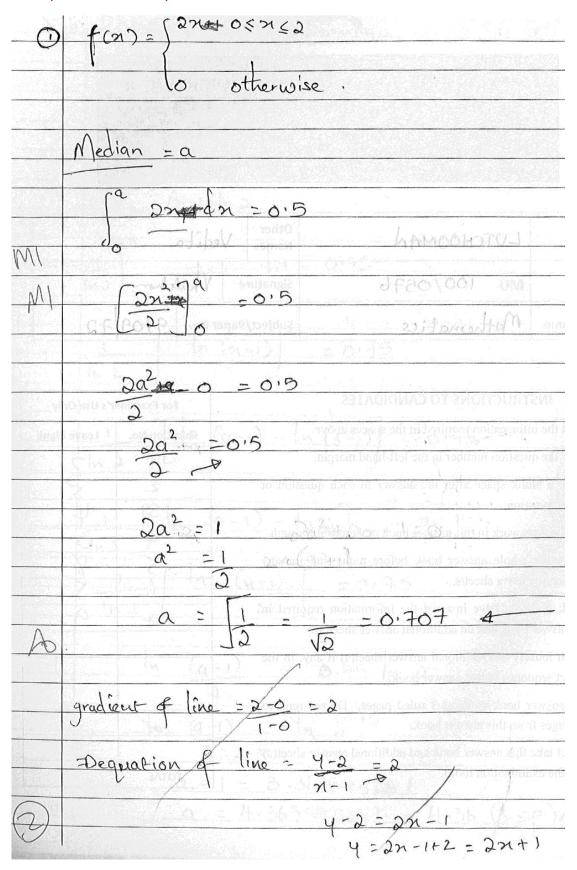
1



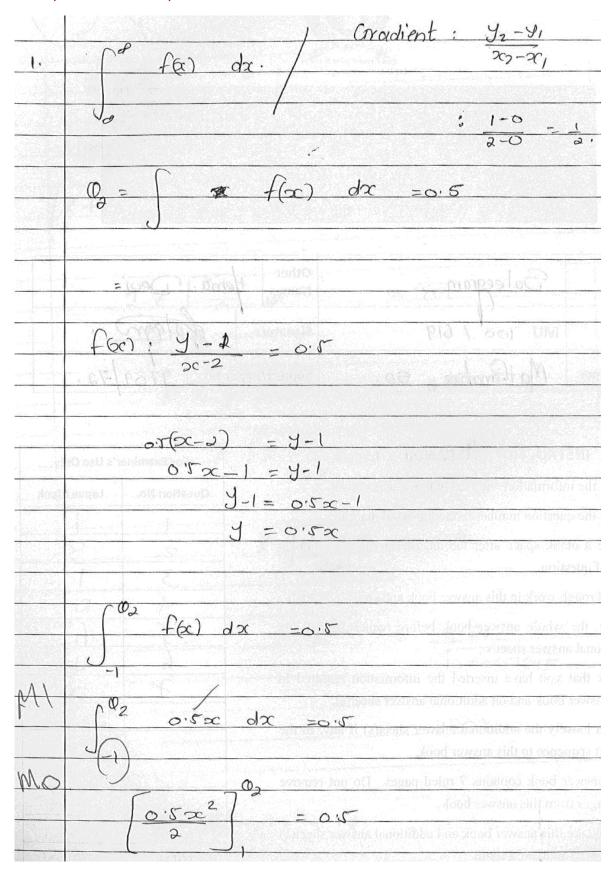
The diagram shows the graph of the probability density function, f, of a random variable X. Find the median of X.

Mark scheme

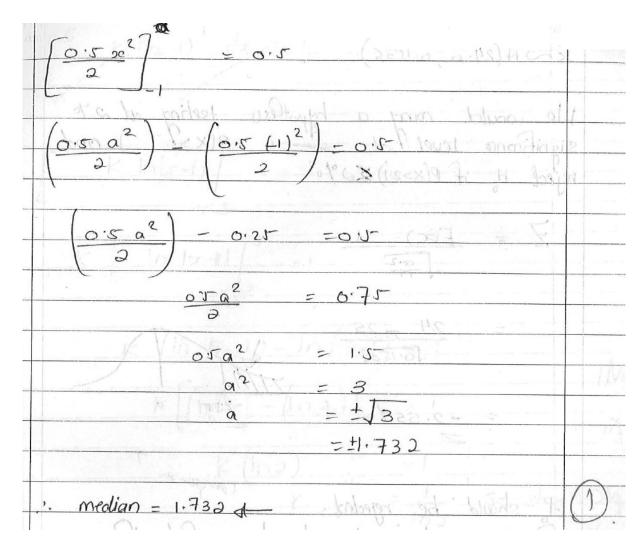
1	$\left(\frac{m}{2}\right)^2$ $\left(\frac{m}{2}\right)^2 = \frac{1}{2}$	M1		$y = \frac{1}{2}x$ (attempt at linear equ with $c = 0$) $\int_{0}^{m} (\frac{1}{2}x) dx = \frac{1}{2}$
	$m = \sqrt{2}$ or 1.41 (3 sfs)	A1.	[3]	(Note: $\pm \sqrt{2}$ as final answer scores A0)



Total mark awarded = 2 out of 3



Example candidate response – 2, continued



Total mark awarded = 1 out of 3

Examiner comment – 1 and 2

Both of the candidates realised the need to find the equation of the straight line between 0 and 2, and both candidates found an equation of the correct form (y = mx).

In order to find the median, it was then necessary to integrate from 0 to 'm' and set this equal to 0.5. Candidate 1 did this correctly and would have gained full marks for the question if their equation of the line had been correct.

Candidate 2 was unable to apply their knowledge to this particular question and made the error of integrating the probability density function from -1 to m and consequently did not gain the method mark for this step of the process.

Question 2

The heights of a certain type of plant have a normal distribution. When the plants are grown without fertilizer, the population mean and standard deviation are 24.0 cm and 4.8 cm respectively. A gardener wishes to test, at the 2% significance level, whether Hiergro fertilizer will increase the mean height. He treats 150 randomly chosen plants with Hiergro and finds that their mean height is 25.0 cm. Assuming that the standard deviation of the heights of plants treated with Hiergro is still 4.8 cm, carry out the test.

Mark scheme

2	H ₀ : Pop mean = 24.0 H ₁ : Pop mean > 24.0	B1	Allow 'μ' but not just 'mean'
	$\frac{25 - 24}{\frac{4 \cdot 8}{\sqrt{150}}}$	M1	Standardise, with √ 150. Ignore ce. Accept sd/var mixes. OR find x _{crit}
	= $2.55(2)$ Comp $z = 2.054$ or 2.055 Evidence that Hiergro has incr hts	A1 M1 A1ft [5]	For correct z or area or x _{crit} Valid comparison (z values/areas/x values) Correct conclusion No contradictions (Note 2 tail test can score B0 M1 A1 M1 (z = 2.326) A1ft)

2.	let # be the random variable of the heights
	of a certain types of plant.
nly	Dell'a sonimext 10 MA ~ H (24.0, 4.82)
Blank	trace the interesting rengined in the spaces above. If the interestion No.
	MAN (24.0, 4.52)
	Ho: M= 25250024,0
- 1	H,: M> 250. 24.0
61	G 155 V n A - 1 G & - 8 Months and a state of the state o
	1f Ho is true, x ~ H (d4.0, 4.82)
	we use a upper tail test at 2% Significance
	Level. I grown for all more below the sufficient states are said.
	100%-2% = 98%
	= 0.98
	= 2.055
	7 = X-0M (= EBISA) Dinnex (Ch
	Z = X-M (HEBISAIDINGX III)
	Th
	7 2- 10
	Z = 25-24 /SHIX 2 - NOON
	V150
	1150
	Z = 2.552 36 x 2 = 3000 10 2
	cost no comp.
Si	nce the test statistic is 2.582, it falls
in	the rejection area therefore we reject Ho Mo
	favour of H.
	3

Total mark awarded = 3 out of 5

2.	let x be the heights of a certain type of Plant	
	let x be the heights of a certain type of plant 18 X ~ N(24.0, 4.8)*	
	$\bar{\chi} = 25$	/9
	8 NO Ho = 24.0 Ha > 24.0 (upper tail	(test)
	Assuming Ho is true, $\overline{R} \times N(24.0, 4.8^2)$ 150	M
	# X ~ N(24.0, 4.83) (SEP) M	(/1)
	150	(1)
	standardization 29 NDA (35) HOLLOMOS ESHU 30 5 49	(11)
	$\bar{z} = (X_0 - M)$	
	TO XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	Λ
	22 MCH+ M+M+M+H+H, OFO+O+O+O+O+O)	
	= 250-24.00 = 1 = 2.552 4.8 200 = 0.3919	ATI
	4.8 1300 = 0.3919 VISO	7.7
	4150	

MOLES.	At 2 % significance level.
	(upper tail)
MO	2.552 70.02
	dtrover we reject to, since themean beight has
	inereased we have enough evidence to prove
1	2/65 that the height has increased.
9	1 = 0 - 3P
0	4 2

Total mark awarded = 2 out of 5

Paper 7

Examiner comment - 1 and 2

Both candidates attempted to define the null and alternative hypotheses. Candidate 1 did this correctly using " μ " to signify the population mean. Candidate 2 wrote that $H_o = 24$ and $H_1 > 24$ without reference to the population mean, and thus did not gain the mark available.

The calculation of the z value was done correctly by both candidates.

Candidate 1 did not then show their comparison, and although the correct conclusion was reached it was not justified. It is important that either the inequality (e.g. 2.552 > 2.054 or equivalent for area comparisons) is stated, or the two points are shown on a clearly labelled normal distribution diagram, so that the conclusion reached is fully justified.

Candidate 2 was unable to gain any marks for their comparison as it was not valid; the candidate compared a *z* value with an area.

Question 3

- 3 The cost of hiring a bicycle consists of a fixed charge of 500 cents together with a charge of 3 cents per minute. The number of minutes for which people hire a bicycle has mean 142 and standard deviation 35.
 - (i) Find the mean and standard deviation of the amount people pay when hiring a bicycle. [3]
 - (ii) 6 people hire bicycles independently. Find the mean and standard deviation of the total amount paid by all 6 people.

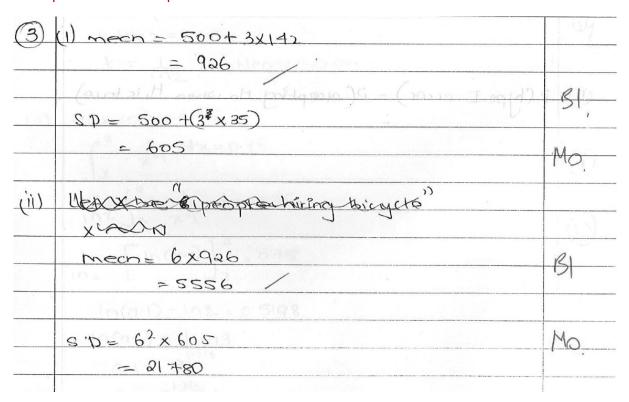
Mark scheme

3	(i)	Mean = 500 + 3 × 142 = 926 (cents)	B1		
		SD = 3 × 35 = 105 (cents)	M1 A1	[3]	Or 9×35^2 seen Accept $\sqrt{11025}$
	(ii)	Mean = $6 \times {}^{\circ}926' = 5556$ (cents) $6 \times {}^{\circ}105'^{2}$ (= 66150) (SD = $\sqrt{66150}$) = 257 (cents) (3 sf)	B1ft M1	[3]	or SD = $\sqrt{6} \times '105'$. ft their (i) Accept $\sqrt{66150}$

503 + 30 00 c + 13c x x x x x x x x x x x x x x x x x x x	1
	and the second s
let Z be diriv amoder of hing a bic	Licyde,
let t be diriv earner of hing a bie	ycle
Le de la strange sur 11 a	4 31
2~N(142,352)	e de la companya de l
X — (100) (100) (100) (100)	
Mean = 500 + 3a	tode
E(2) = E(500) + E(301)	
(= x)4+ (= 500 + (3 E(x)) () () () () () ()	
500 + 3 (142)	11.07
	/ BILL
900 C STANDARD (1800)	//8
Var (2) - Var (200) 1 Q Var (2)	0
Var (2) = Var (500) + 9 Var (x)	1902 140 ON
Var (2) = 19(1025) Habrier from The	-00
Var(2) = 11005	MI
11,025 (12 X)9	An
- 105 A / PA	///.
Mr. 60.0 + F1800.0 = ,	
(11) 6 people hire independently	
let V bediriv 6 people hire bicycles"	120.
1	
0-1	(10)
	19
5,556 M = 680: All	24/
The sound of the s	DI'.
# 1.68/35 Q - 1.68/35 /	MO
0 = 3.379	

Item marks awarded: (i) = 3/3; (ii) = 1/3

Total mark awarded = 4 out of 6



Item marks awarded: (i) = 1/3; (ii) = 1/3

Total mark awarded = 2 out of 6

Examiner comment – 1 and 2

(i) Both candidates 1 and 2 were able to correctly find the mean.

To find the standard deviation the correct calculation was performed by candidate 1, but candidate 2, incorrectly, added 500.

(ii) Again, both candidates 1 and 2 correctly found the mean, but neither found the correct variance.

Candidate 1 calculated $6 \times$ standard deviation rather than $6 \times$ variance (it may have been their intention to calculate $6 \times$ variance, but unfortunately this was not what the candidate actually did). Candidate 2 was not clear about what was required and calculated $6 \times$ their standard deviation.

Question 4

- 4 A cereal manufacturer claims that 25% of cereal packets contain a free gift. Lola suspects that the true proportion is less than 25%. In order to test the manufacturer's claim at the 5% significance level, she checks a random sample of 20 packets.
 - (i) Find the critical region for the test. [5]
 - (ii) Hence find the probability of a Type I error. [1]

Lola finds that 2 packets in her sample contain a free gift.

(iii) State, with a reason, the conclusion she should draw. [2]

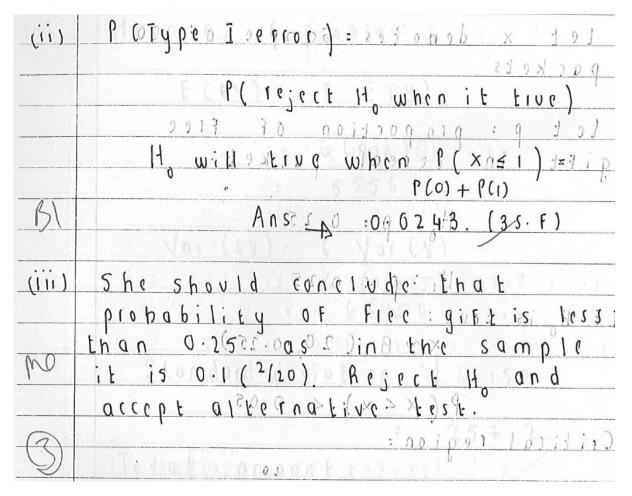
Mark scheme

4	(i)	$P(X \le 1) = (0.75)^{20} + 20(0.75)^{19}(0.25)$ = 0.0243	M1 A1		Attempt correct expression
		$P(X \le 2) = (0.75)^{20} + 20(0.75)^{19}(0.25) + \frac{^{20}C_2(0.75)^{18}(0.25)^2}{0.0913 \text{ or } 0.0912}$	M1 Al		Attempt correct expression OR Find P(2) = 0.0669 or 0.0670
		Critical region is 0 or 1 pkt contain gift or < 2 pkts contain gift oe	A1 [[5]	dep M1M1 & their $P(X \le 1) < 0.05 <$ their $P(X \le 2)$ (S.R. Use of Normal: N(5.3.75 ²) used B1 $-1.645 = (x + 0.5 - 5)/\sqrt{3},75 \text{ M1}$ $x < 1.31 \text{ A1}$ (3/5))
	(ii)	P(Type I) = 0.0243 (3 sfs)	Blft [[1]	ft their $P(X \le 1)$ dep < 0.05 ft Normal
	(iii)	2 is outside rej reg No evidence to reject claim	Ml Alft [[2]	or $P(X \le 2) > 0.05$ No contradictions

Sol:-	this margin
i Let x denotes : sample so fg p20	9 (ii)
packets	
P(10ject 11 when it true)	
Let p: proportion of free	
giftet (12hx) & e negative pacike time of	
Anst 100 00: 04 250 1).	T/A
1 .2 1 / = 0 - 75	
hershould tono 1 x do: Hhad E	(iii) S
IFOH issi thue: 2017 70 prilidador	9
119 m 0 8 1×1× Bni(20,00.257)5.0 no	h
DUD H 1333 34 - 1034 D1403 C1	11 47
. P2(x < x) 1 (n 0 0 0 5 1 D 1 9 0 0 0	D
Critical region:	
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
P(0): (20) (0.25) (0.15) -:/	5) 50
F(3c): k 3 6 3c 6 5	(i)
0.003,47,000	
19 80	
P(1) = 120 1 (0.25) (10.75)	
2 - Andrew X	Mo.
: 0.02114	
7 3 191.25	
P(2): (20) = (0.[25]) = (0.75]) x	
2 1 18 4 11 2 0 1	MIAI
: 0.0669	
P(0) + P(x) + P(x) >> - 01.008 >	
$\frac{1}{1} = \frac{1}{1} + \frac{1}$	1
(1 > x) 29 11 2 2 A	Jeg J

Paper 7

Example candidate response - 1, continued



Item marks awarded: (i) = 2/5; (ii) = 1/1; (iii) = 0/2

Total mark awarded = 3 out of 8

noguan	Question 4	i e
	let x be the riv, "a cereal manufacturer claiming cereal"	
	(SEERI) HOX packets	
	x ~ B (20, 0.25)	
	H. < 0.25 (Reject H.) H. 70,25 (Accept H.)	
(i)	P(Type I error) = P (Reject H / H is true)	
	= P (H <0.25) / (20,0.25)) bushole	
1-0	(a) = 0.05 T 85H 9 5×8 =	
	a)=0.95 = lerel of significance	
	7 = 1.645 = 1.645	U
	= 8.4148 (critical region)	
	p (x < 0,25) < 5 % -7 Reject H	
	20c (0.25) (0.75) 20+ 20c (0.25) (0.15) + mosni	Ī
	20c (0,25) 2 (0,15) + 20c (0,25) 3 (0,15) 17+	A STATE OF THE PERSON NAMED IN
MO	$20c(0.25)^{6}(0.75)^{20} + 20c(0.25)^{6}(0.75)^{17} + 10000$ $20c(0.25)^{2}(0.75)^{18} + 20c(0.25)^{3}(0.75)^{17} + 20c(0.25)^{4}(0.75)^{16} + 20c(0.25)^{5}(0.75)^{15} + 20c(0.25)^{6}(0.75)^{17}$	9
MO	+20c1 (0.25)1 (0.75)13+20c8 (0.25)8 (0.75)12+20c9 (0.25)9 (0.75)	t
	+2090(0.25)10(0.75)0+2061 (0.25)1 (0.75)9	
(11)	Trype Ilmor) = 1.695	
0	et it be the 6 people	(
150	MVH (6x426) 6x105)	
(14)	This means that there is significant evidence as it does	
Cat-ministry (A.)	ties below not lie in the critical region (25 + x 2) = about	
Mo	305 6	
\bigcirc		
(0)	Signatural deviation = (EXIDS) +500	

Item marks awarded: (i) = 0/5; (ii) = 0/1; (iii) = 0/2

Total mark awarded = 0 out of 8

Examiner comment – 1 and 2

(i) Finding the critical region was not, in general, well attempted.

Candidate 1 used B(20,0.25), but calculated P(0), P(1), and P(2) separately without combining the probabilities to find $P(X \le 1)$ and $P(X \le 2)$, so although the candidate identified the correct critical region (although not expressed correctly) full justification (i.e. $P(X \le 1) = 0.0243 < 0.05$ and $P(X \le 2) = 0.0913 > 0.05$) was not shown.

Candidate 2 also used B (20, 0.25), but did not calculate any relevant probabilities and used 1.645 (a normal distribution value).

(ii) Candidate 1 correctly found the probability of a Type I error (0.0243) from previous working.

Candidate 2 gave an answer of 1.645 which, for a probability, could not have been correct. It is important that candidates always think about how sensible their answers might be.

(iii) In general, candidates on this part of the question did not draw conclusions relating back to the test.

Candidate 1 had the correct critical region and could have gained marks here by realising that '2' was not in the critical region. However, no marks were gained.

Although candidate 2 did make reference to the critical region, no justification for their (vague) statement was made. Candidates should be specific with comparisons; "it" does not lie in the critical region is too vague.

Question 5

5 A random variable X has probability density function given by

$$f(x) = \begin{cases} \frac{k}{x-1} & 3 \le x \le 5, \\ 0 & \text{otherwise,} \end{cases}$$

where k is a constant.

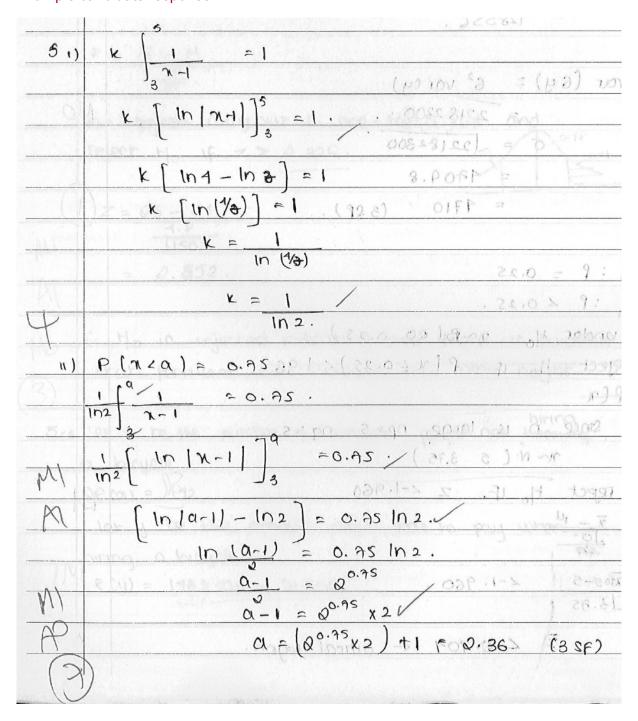
(i) Show that
$$k = \frac{1}{\ln 2}$$
.

(ii) Find *a* such that P(X < a) = 0.75.

Mark scheme

5	(i)	$\int_{3}^{5} \frac{k}{x-1} dx = 1$ $[k \ln(x-1)] \frac{5}{3} = 1$ $k(\ln 4 - \ln 2) = 1$ $k \ln 2 = 1$ $(k = \frac{1}{\ln 2} \mathbf{AG})$	M1 A1 M1 A1 [4]	Attempt integ $f(x)$ & '= 1' ignore limits Correctly integrated; ignore limits Subst of limits 3, 5
	(ii)	$\frac{1}{\ln 2} \int_{3}^{x} \frac{1}{x \cdot 1} dx = 0.75$ $\frac{1}{\ln 2} \left[\ln(x - 1) \right]_{3}^{x} = 0.75$	M1*	No errors seen. No decimals seen Attempt integ $f(x)$, unknown limit, & '= 0.75' or '= 0.25'
		$\frac{1}{\ln 2} (\ln(x-1) - \ln 2) = 0.75$ $\ln (x-1) = (0.75 \times \ln 2 + \ln 2)$ $\ln (x-1) = 1.75 \times \ln 2$	AI	oe. Fully correct equn after subst limits
		$x-1 = 2^{1.75}$ or $x-1 = 3.36$ x = 4.36 (3 sfs)	M1 dep* A1 [4]	oe. Correct manipulation of logs to find x

Paper 7



Item marks awarded: (i) = 4/4; (ii) = 3/4

Total mark awarded = 7 out of 8

Question 5.	0.3603	In (a-1) =	this margi
	9 .360 33 Tr	= 1-0	
(1)	2.43	n D	
J3 2-1			1
			15/
$ K \ln(x-1) ^{3} = 1$		Sizstion 6	- V2/
[]3/	(Arean Const. 19 and 19 and		MI
aldood have see told so			A. /
K 1911 4 - 112 300 52 100	qual chance of hei	will have then e	AL
			nAı
ACTIVO. SAMBLEO , COM	Signature	(Aumorp.	1011
K (1n4) = 61	h dences intervell	Atteggth con	(11)
[Inz]			
(4)	= PS ± 2,326	bb.0=(v)	AO
In 2 k = 100000		tion Examina (D) (Inly
1. It sen the information required in the space		Question No. Lea	Ae Blank
2. Williams (Society) (Soc	= 38 1 7/3 x		
per of question			1-27
(11) $P(X < Q) = 0.75$	Later & description		_ (_/\text{\tin}\text{\tin}\text{\tex{\tex
26952 ps	= 38 ± 0.0		II /A
$\frac{1}{100} = 0.75$ $\frac{1}{100} = 0.75$			
1/12 J3 2 - 1/2 inserted the inform			H-QA
7. Adams sousely the additional areas their	0.75		
COLECT SOLITER COLD MINISTERIOR	0.19		
any pages from this answer sook.	Do get move		MI
	S. 75		M
$\frac{1}{\ln 2} \left[\ln (\alpha^{-1}) - \ln 2 \right] = 0$	0113	4	M .
	1986		
$\frac{\pi \eta(\alpha 1)}{\ln 2} = 0.5$	7760		MO

Paper 7

Example candidate response – 2, continued

Question No.	$\ln (a-1) = 0.3603$ $a-1 = e^{0.36033976}$		westion s	Nothing is to be written in this margin
	a-1 = e 0.360 33976			•
L4	Q = 2.43	= 1.	l k	(1)
			13 2-1	
(>)				

Item marks awarded: (i) = 3/4; (ii) = 2/4

Total mark awarded = 5 out of 8

Examiner comment - 1 and 2

(i) Candidate 1 scored full marks on this part.

Candidate 2 knew the correct method to use to find k, but made an error in their manipulation of the logarithmic expression. Whilst the candidate reached the correct value of k it was not legitimately obtained and therefore did not score the final accuracy mark.

(ii) Candidate 1 was able to integrate correctly using the correct limits and would have scored full marks but unfortunately made a re-arrangement error, on the last line, when solving the equation to find *a*.

Candidate 2 also had a correct method to find a, using the correct integration and correct limits, but as in part (i), showed a misunderstanding of logarithms by stating that $\ln(a-1) - \ln 2$ was equal to $\frac{\ln(a-1)}{\ln 2}$

Question 6

- 6 In order to obtain a random sample of people who live in her town, Jane chooses people at random from the telephone directory for her town.
 - (i) Give a reason why Jane's method will not give a random sample of people who live in the town. [1]

Jane now uses a valid method to choose a random sample of 200 people from her town and finds that 38 live in apartments.

- (ii) Calculate an approximate 99% confidence interval for the proportion of all people in Jane's town who live in apartments. [4]
- (iii) Jane uses the same sample to give a confidence interval of width 0.1 for this proportion. This interval is an x% confidence interval. Find the value of x. [4]

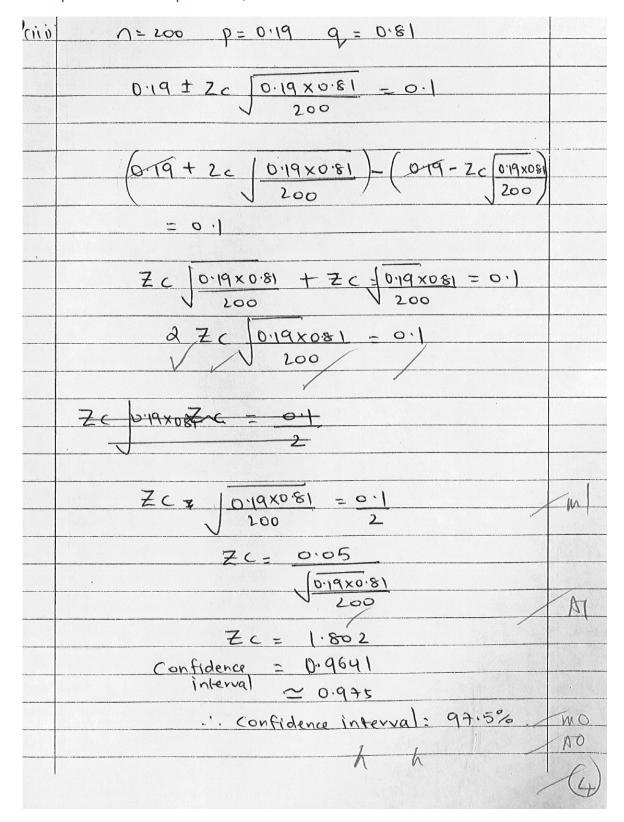
Mark scheme

6	(i)	Excludes children Excludes people without phones More than one person in some houses Some ex-directory	B1	[1]	or other implying directory excludes some people
	(ii)	$Var(p) = \frac{\frac{38}{200}(1 - \frac{38}{200})}{200} (= 0.0007695)$ $z = 2.576$ $\frac{38}{200} \pm z \sqrt{\frac{\frac{38}{200}(1 - \frac{38}{200})}{200}}$ $0.119 \text{ to } 0.261 \text{ (3 sfs)}$	5) M1 B1 M1 A1		Seen For correct form of Cl Accept 0.262 Must be an interval
	(iii)	$z \times \sqrt[4]{0.0007695}$ = 0.05 z = 1.802 $\Phi(1.802)$ (= 0.9642) (0.9642) - (1 - 0.9642) = 0.9284 x = 93 (2 sfs)	M1 A1 M1		$z \times (\text{their sd of } p) = 0.05$. Allow = 0.1 Attempt $\Phi(\text{their } z)$ and find $2\Phi - 1$

Paper 7

6.	(i) Jane's method will not give a random
	Sample because people in the chas that
	She has chosen from the belephone
80	directory may not live in the town.
/	Since I is a caper than to literate from
	69/majx pragis 31 applications to possing and
_ (ii)	
	n = 200 p = 38 $q = 1 - 38$ 200
	(p=10019 - 79 = 0.81
	99% = 0.99
	Zc = 2-326.
ml	Ps + Re Zc. Psqs (26)
20	Vn
80	0.19 ± 2-326 10.19x0.81
m1 -	0.19 ± 2-326 0.19x081
۸ -	(0.125; 0.255)
AD	-> d f 0 0
	0.125 < p < 0.255 '

Example candidate response – 1, continued



Item marks awarded: (i) = 0/1; (ii) = 2/4; (iii) = 2/4

Total mark awarded = 4 out of 9

	Question 6	Ţ =	(1-X	K In (
(8 .	J
(1)	Because this method is	biased as 70	it eo every	people
0	will have the equal chance	of being, select	ted in the	sample.
150	7			7
MAN	RO Y	significance		
(11)	At 99% confidence inte	ral	regions	
- C)/-	$\phi(a) = 0.99 = Ps \pm$	2.326 / Ps9	5	X
	Φ(a)=	1 200		P 1000
		UMDUS (0.52)	(K 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1	*
	= 38	± 21326 /(38/200)(16/2	000
Bo	200	1.7	200)
100	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	75	0 = (p	> X) «
TO TO	= 38	± 0.06952	1	
MI	200	oris	= 1	N. D.)
				راع ۶
10.	is record that there is	, 0·125 < H <	0.255	TE Obest
61	ES REST CARE AND DECEMBER	0.75	(1-x) (1	17
6		3		12
(2)				
W.	1/			7
(11)	22 (2) 1 - (21)		500-1-	1991
_	20(2)-1=(0·1)			
MO,	$\varphi(x) = 1.1$ $\varphi(x) = 0.55$	<u> </u>	rn5n7	
Λ.Ο		3	× HED	
MO,	x = 0.125			
	?, x = 12.5%	01	= \(\(\lambda\) (1)	
6)	2 / Z / / Z / Z			11

Item marks awarded: (i) = 0/1; (ii) = 2/4; (iii) = 0/4

Total mark awarded = 2 out of 9

Examiner comment - 1 and 2

- (i) Neither candidate was able to give a correct reason for why Jane's method would not work. The method described did not allow equal chance of being selected because, for example, it excludes people without phones. A valid reason was required.
- (ii) Both candidates made similar errors in finding the confidence interval. Whilst the general method was correct, both candidates 1 and 2 calculated the *z* value incorrectly. Both looked up 0.99 to get a *z* value of 2.326, whereas for a 99% confidence interval 0.995 should have been looked up on the tables to get a *z* value of 2.576. This resulted in two marks not being awarded to both candidates.
- (iii) Candidate 1 formed a correct equation, leading to the correct *z* value of 1.802. However, the candidate did not find the correct percentage for the confidence interval.

Candidate 2 was unable to set up a correct initial equation to find z.

Paper 7

Question 7

- 7 A random variable X has the distribution Po(1.6).
 - (i) The random variable R is the sum of three independent values of X. Find P(R < 4). [3]
 - (ii) The random variable S is the sum of n independent values of X. It is given that

$$P(S = 4) = \frac{16}{3} \times P(S = 2).$$

Find
$$n$$
. [4]

(iii) The random variable T is the sum of 40 independent values of X. Find P(T > 75). [4]

Mark scheme

7	(i)	$\lambda = 4.8$ $E^{-4.8}(1 + 4.8 + \frac{4.8^2}{2!} + \frac{4.8}{2!} $	8 ³ 3!	B1 M1 A1	[3]	$P(R = 0, 1, 2 \text{ or } 3)$, their λ allow one end en	ror
	(ii)	$e^{-\lambda} \times \frac{\lambda^4}{4!} = \frac{16}{3} e^{-\lambda} \times \frac{\lambda^2}{2!}$ $\frac{\lambda^2}{12} = \frac{16}{3}$ $(\lambda = 8)$ $\lambda = 1.6n \text{ seen or implied}$ $n = '8' \div 1.6$ $= 5$	or better	M1 A1 B1 A1	[4]	$\lambda = 1.6n$ seen or implied B1 $e^{-1.6n} \times \frac{(1.6n)^4}{4!} = \frac{16}{3} e^{1.6n} \times \frac{(1.6n)^2}{2!}$ M1 $\frac{(1.6n)^2}{12} = \frac{16}{3}$ or better A1 $(1.6n = 8)$ $n = 5$ A1	
	(iii)	$T \sim N(64, 64)$ $\frac{75.5 - 64}{\sqrt{64}}$ $1 - \Phi('1.4375')$ = 0.0753 to 0.0754	(= 1.4375) (= 1 – 0.9247)	B1 M1 M1 A1	[4]	May be implied Allow with wrong or no cc. No sd/var mix Finding correct area consistent with their working	es

5	x~Po (1.0)	(0)
1)		
5	3n Po (4-8)	
	P(R64)= lo +l, +lo +la	
	P(R < 4) = lo +l, +l2 + l3 = e-4.8 (1+4.8 +4.82 + 4.83)	6
	21 31	
0	= 0.29u.	
5		
(P)	P(S=u) = e-1.60 = e-1.60 4 4!00 = e-1.60 4 2u	
	4!000 20	
115	$P(S=2) = \frac{e^{-1.67} \cdot 1.67^2}{0!} = \frac{e^{-1.67 \cdot 1/.67^2}}{2}$	
	2:	
	1.0 -2 / 1.0 - 1.0 - 1.0	Con
	$\frac{2^{-1.6}}{\times 1.60} = \frac{16}{3} \times e^{-1.60}$	
	41 3 21	
01	512 e-160 675 e-160	
151	1875	
1	$e^{-1.60} \times 1.60^4 = 16e^{-1.60} \cdot 1.60^2$ (x2)	رب)
	24 202	
	e-1.60 × 1.604 = 128 × (e-1.60 = 1602)	t/169
Alleria de la composición del composición de la		201
2/7/10	$Q^{-\alpha} \times \alpha Q^{\alpha} = (08 (12(e^{-\alpha}, \alpha^2)))$	
DD	9 0-9 = 128 (10201202 e-9)	
N .	a ⁴ e ^{-a} = 1536 a ² e ^{-a} = e ^{-a}	
- Br.	$q^2 = 1536$.	
	$\alpha = 39.192$ $1.60 = 39.192$	
	05 N=24 N=24.49	

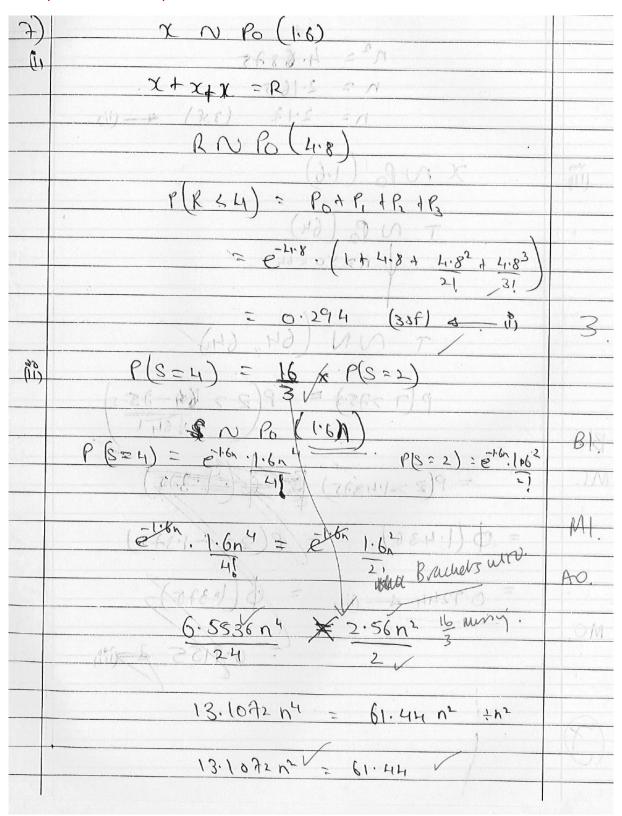
Paper 7

Example candidate response – 1, continued

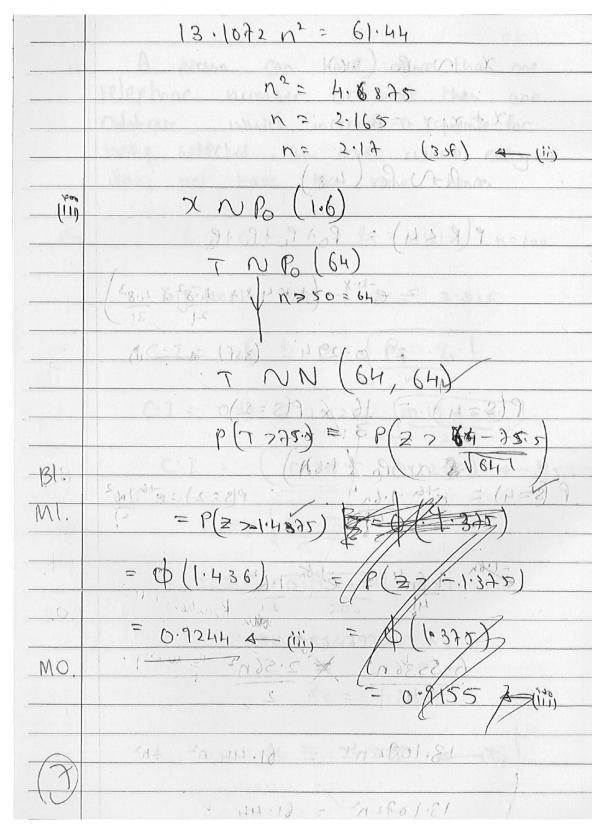
Sir)	A-409	
	As 1>15, XN (64, 64)	BI
	2=7x-60 V(T) 760	
	P(T>75) Tou	
	P(2>75-64)	MI
	Vou .	MI
	= (- \beta (1.375)	AO,
	> 0.08u5	1,
		(2)
		0

Item marks awarded: (i) = 3/3; (ii) = 2/4; (iii) = 3/4

Total mark awarded = 8 out of 11



Example candidate response – 2, continued



Item marks awarded: (i) = 3/3; (ii) = 2/4; (iii) = 2/4

Total mark awarded = 7 out of 11

Examiner comment - 1 and 2

- (i) Both candidates were able to identify the value of λ to use (4.8) and then correctly to find the required probability.
- (ii) Both candidates at both grades were able to set up the correct equation and use $\lambda = 1.6n$. They both tried to solve this equation to find n, but neither successfully reached n = 5.
 - Candidate 1 made an early error when rearranging their equation, and candidate 2, whilst initially having used the given value of 16/3 in their equation, missed this value out in later working.
- (iii) Candidate 1 used the correct distribution N(64,64) to find the required probability, but omitted to use the required continuity correction.
 - Candidate 2 also used N(64,64), but found $\phi(z)$ rather than $1-\phi(z)$. A normal distribution diagram may have helped this candidate realise that their final answer should have been smaller than 0.5, thus avoiding the error made.

